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- **Authentic exam practice:** Develop your exam technique and time management skills with realistic papers mirroring the latest syllabus and exam format.
- **Targeted content:** Strengthen your understanding across all key topic areas, with a focus on areas predicted to appear in the 2025 exams.
- **Detailed solutions:** Gain valuable insights into effective problem-solving approaches and reinforce your learning with comprehensive, step-by-step solutions.

Boost your confidence and achieve your full potential in the iGCSE Maths examinations with this essential resource!



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MATHEMATICS

0580/21

Paper 2 Non-calculator (Extended)

February/March 2025

2 hours

You must answer on the question paper.

You will need: Geometrical instruments

INSTRUCTIONS

- Answer **all** questions.
- Use a black or dark blue pen. You may use an HB pencil for any diagrams or graphs.
- Write your name, centre number and candidate number in the boxes at the top of the page.
- Write your answer to each question in the space provided.
- Do **not** use an erasable pen or correction fluid.
- Do **not** write on any bar codes.
- Calculators must **not** be used in this paper.
- You may use tracing paper.
- You must show all necessary working clearly.

INFORMATION

- The total mark for this paper is 100.
- The number of marks for each question or part question is shown in brackets [].
For extra guidance, use the [All of iGCSE Maths Playlist](#)

List of formulas

Area, A , of triangle, base b , height h .

$$A = \frac{1}{2}bh$$

Area, A , of circle of radius r .

$$A = \pi r^2$$

Circumference, C , of circle of radius r .

$$C = 2\pi r$$

Curved surface area, A , of cylinder of radius r , height h .

$$A = 2\pi rh$$

Curved surface area, A , of cone of radius r , sloping edge l .

$$A = \pi rl$$

Surface area, A , of sphere of radius r .

$$A = 4\pi r^2$$

Volume, V , of prism, cross-sectional area A , length l .

$$V = Al$$

Volume, V , of pyramid, base area A , height h .

$$V = \frac{1}{3}Ah$$

Volume, V , of cylinder of radius r , height h .

$$V = \pi r^2 h$$

Volume, V , of cone of radius r , height h .

$$V = \frac{1}{3}\pi r^2 h$$

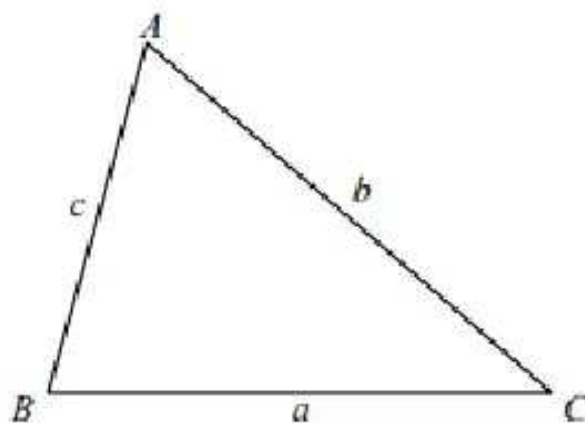
Volume, V , of sphere of radius r .

$$V = \frac{4}{3}\pi r^3$$

For the equation $ax^2 + bx + c = 0$, where $a \neq 0$,

$$x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$$

For the triangle shown,



$$\frac{a}{\sin A} = \frac{b}{\sin B} = \frac{c}{\sin C}$$

$$a^2 = b^2 + c^2 - 2bc \cos A$$

$$\text{Area} = \frac{1}{2}ab \sin C$$

Calculators must **not** be used in this paper.

- 1 Work out $\frac{4}{9} \times \frac{27}{20}$.

Give your answer as a fraction in its simplest form.

..... [1]

- 2 Write down the order of rotational symmetry of a parallelogram.

..... [1]

- 3 Convert 22400 cm² into m²

..... m² [2]

- 4 John has a biased 6-sided die.

Number	1	2	3	4	5	6
Probability	0.10		0.25	0.20	0.30	0.10

John rolls the die.

Calculate the probability that it lands on a prime number.

.....[3]

- 5 Find the value of $343^{\frac{2}{3}}$.

..... [2]

6 Find the Highest Common Factor (HCF) of 51 and 119

..... [2]

7 y is inversely proportional to $(x + 1)^3$

When $x = 1$, $y = 0.5$

(a) Calculate the value of y when $x = 3$.

$y =$ [4]

(b) Find the value of x when $y = \frac{1}{16}$.

$x =$ [3]

8 **(a)** Simplify.

$$\sqrt{8} + \sqrt{50}$$

..... [2]

(b) Rationalise the denominator:

$$\frac{1}{\sqrt{3}+1}$$

..... [2]

9 **Without using a calculator**, work out $3\frac{2}{7} + \frac{5}{4}$.

You must show all your working and give your answer as a mixed number in its simplest form.

..... [3]

A speed-time graph for a car. The vertical axis is labeled 'Speed (m/s)' and has a tick mark at 30. The horizontal axis is labeled 'Time (seconds)' and has tick marks at 0 and 15. The graph starts at the origin (0,0), increases linearly to the point (15, 30), and then continues as a horizontal line at 30 m/s for the remainder of the time shown.

(a) Calculate the acceleration for the first 15 seconds.

Find the value of T .

$$\frac{1}{2} \times b \times h$$

$$\frac{1}{2} \times 15 \times 30 = 225 \text{ m}$$

$$= 35775 \text{ m}$$
$$35775 - 225 = 35550 T = \dots\dots\dots 19.75 \dots\dots\dots \text{min} [4]$$

11 The scale of a map is 1 : 2000.

The area of a road is 400m^2 .

Calculate the area of the road on the map, giving your answer in cm^2 .

 $1\text{ cm} : 2000\text{ cm}$

20 m

$$1\text{cm}^2 : 400\text{m}^2$$

1cm : 20m

$1 \text{ cm}^2 : 400 \text{ m}^2$

 1 cm^2

..... cm² [3]

12

- (a) Dina invests \$2000 in an account that pays simple interest at a rate of $r\%$ per year.

At the end of 3 years, the account has earned \$300 in **interest**.

Calculate the value of r .

$r = \dots\dots\dots [3]$

(b)

- (i) Hence, or otherwise, calculate the total value of her investment after 6 years.

\$..... [2]

- (ii) Marcus invests \$2500 in a bank which pays simple interest at a rate of 2% per year.

At the end of 6 years, whose investment is most valuable? Give a comparison to justify your answer.

.....

 [2]

13

A is the point $(5, -5)$ and B is the point $(9, 3)$.

(a) Find the coordinates of the midpoint of AB .

(.....) [2]

(b) Find the length of AB .

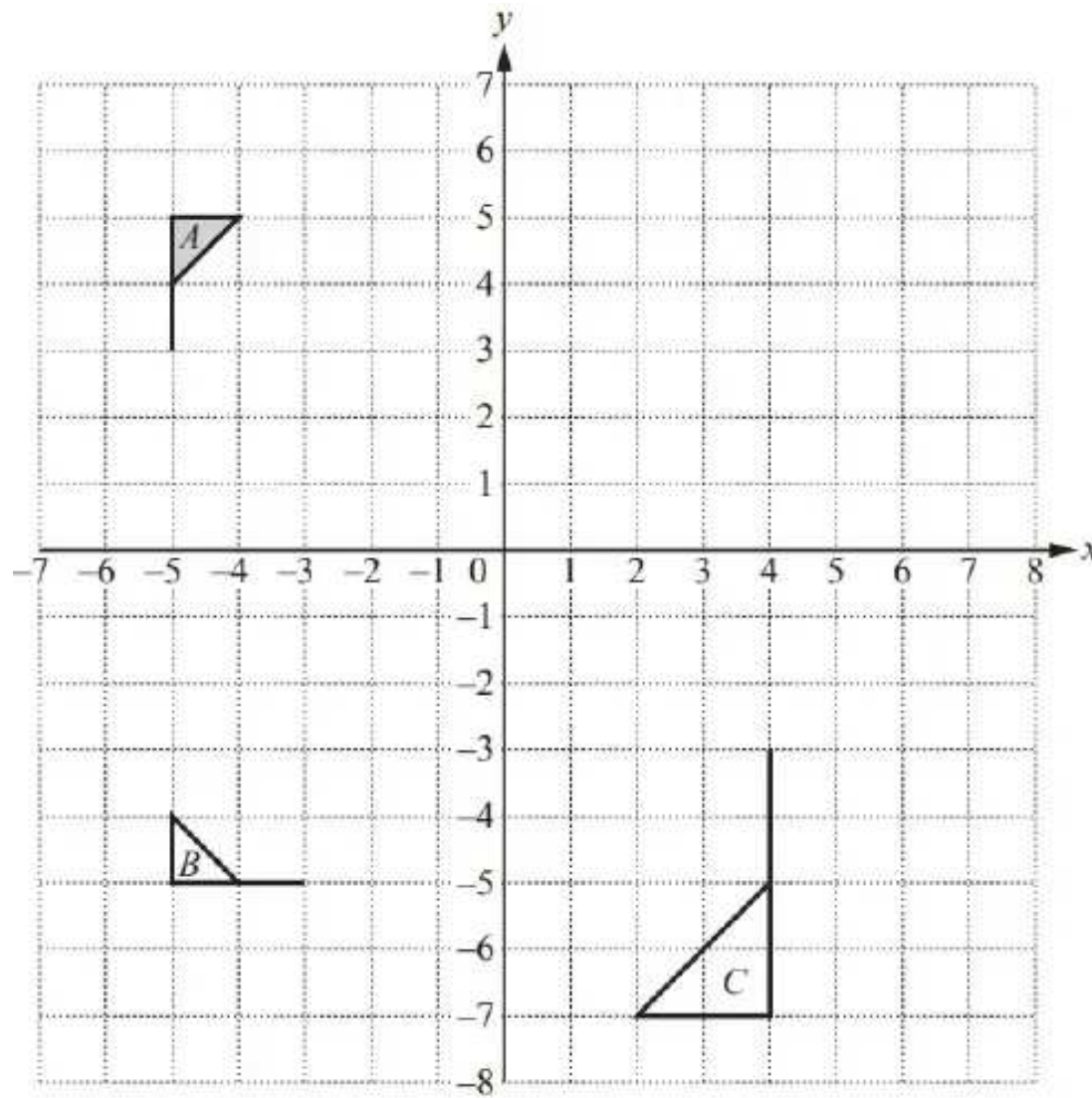
Give your answer in exact form.

..... [3]

(c) Write down the gradient of a line that is perpendicular to the line AB

..... [2]

14



(a) Describe fully the **single** transformation that maps

(i) Flag B onto Flag A,

.....
 [3]

(ii) Flag A onto Flag C,

.....
 [3]

15 Simplify: $\frac{2x^2+5x-12}{4x^2-9}$

..... [4]

16

(a) x is an integer.

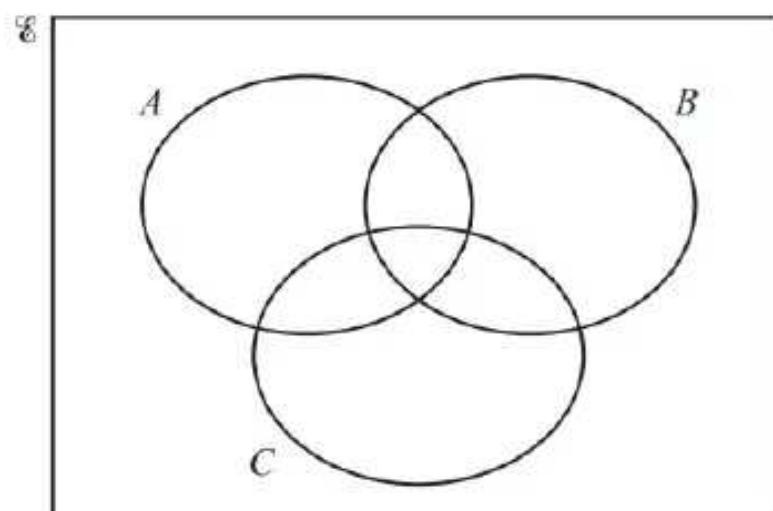
$$\mathcal{E} = \{x: 1 \leq x \leq 10\}$$

$$A = \{x: x \text{ is a factor of } 12\}$$

$$B = \{x: x \text{ is an odd number}\}$$

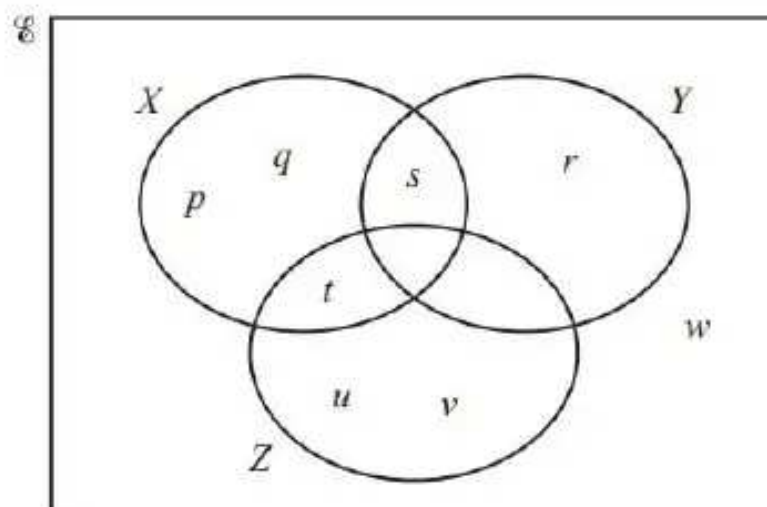
$$C = \{x: x \text{ is a prime number}\}$$

(i) Complete the Venn diagram to show this information.



[3]

(b)



(i) Use set notation to complete the statement.

$\{u, v\} \subset (X \cap Y) \cap Z$

[1]

(ii) Shade $X \cap (Z \cup Y)'$.

[1]

- 17 A plane leaves airport A and flies 8 km on a bearing of 090° to reach point B. From point B, it changes direction and flies 6 km on a bearing of 180° to reach point C.

(a) Calculate the distance from point A to point C.

.....km [3]

(b) Given that $\sin^{-1}\left(\frac{4}{5}\right) = 53.1^\circ$, determine the bearing of point C from point A.

..... [3]

18 Find the n th term of each of the following sequences:

(a) 2, 5, 8, 11, 14, ...

..... [2]

(b) -2, 2, 8, 16, 26, ...

..... [3]

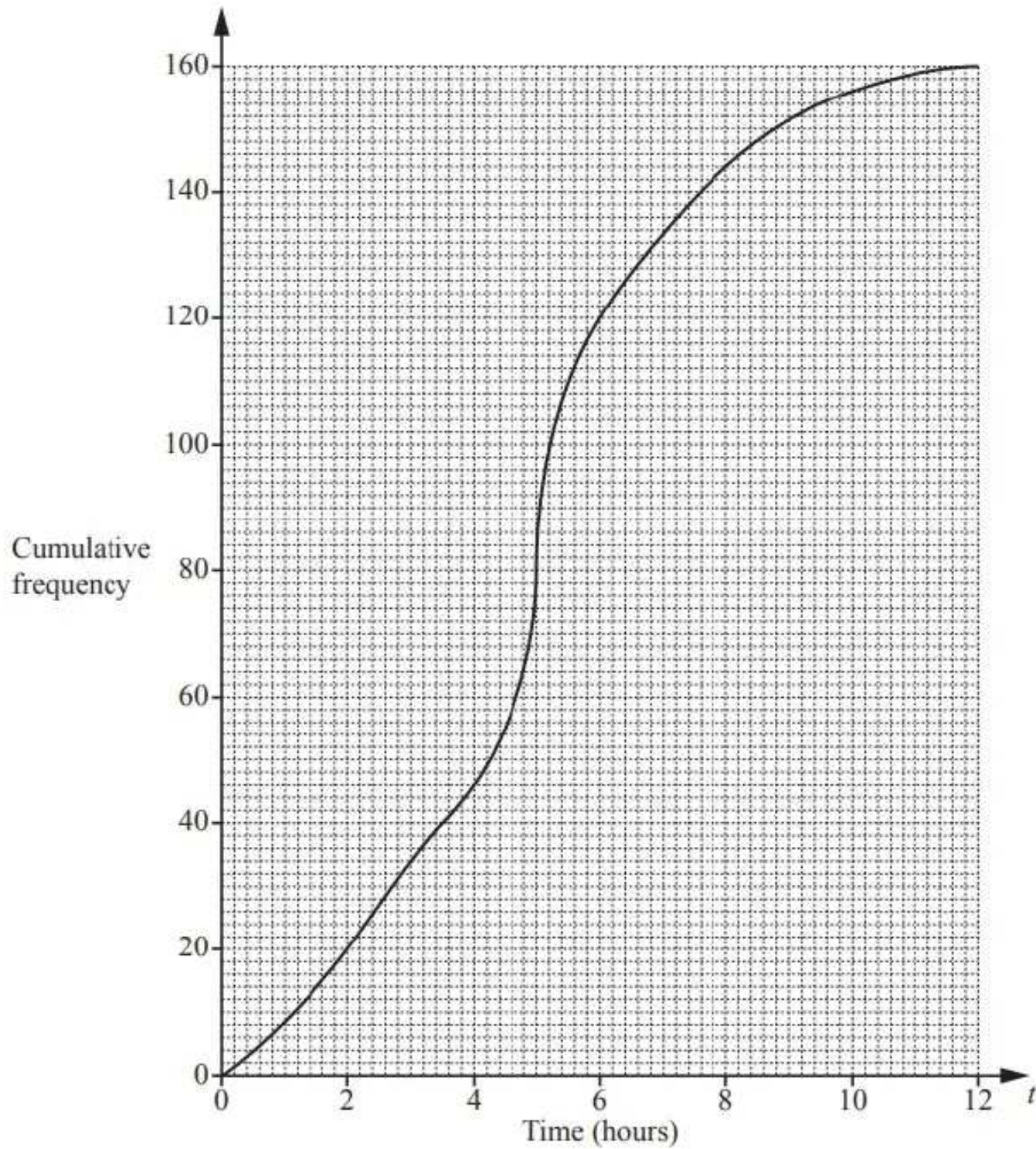
19 Calculate the area of a semicircle with diameter 10cm.

Give your answer in exact form.

..... [3]

20

160 students record the amount of time, t hours, they each spend playing computer games in a week. This information is shown in the cumulative frequency diagram.



(a) Use the diagram to find an estimate of

(i) the median,

.....hours [1]

(ii) the interquartile range,

.....hours [2]

(b) Use the diagram to complete this frequency table.

Time (t hours)	$0 < t \leq 2$	$2 < t \leq 4$	$4 < t \leq 6$	$6 < t \leq 8$	$8 < t \leq 10$	$10 < t \leq 12$
Frequency	20			24	12	4

[2]

21

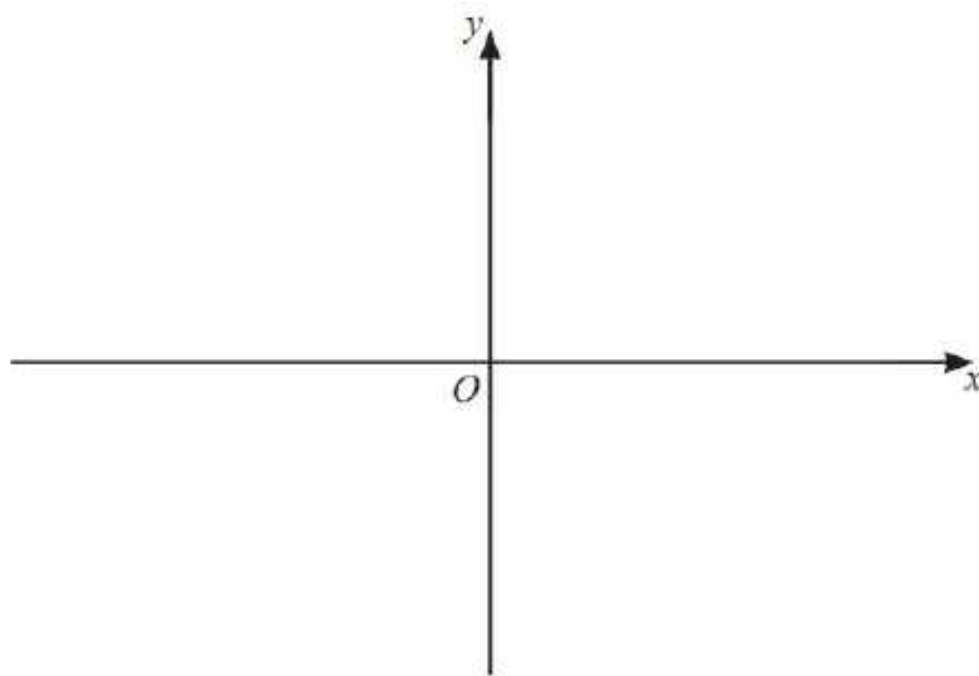
(a) Write $x^2 - 8x + 12$ in the form $(x - a)^2 + b$.

..... [2]

(b) Hence, write down the coordinates of the turning point of the graph of $y = x^2 - 8x + 12$.

(..... ,) [1]

(c)



2

On the diagram, sketch the graph of $y = x^2 - 8x + 12$.

[3]

22 Solve the simultaneous equations.
You must show all your working.

$$\begin{aligned} 2x^2 + 3y &= -8 \\ \frac{4}{3} + y &= -2x \end{aligned}$$

$$\begin{aligned} x &= \dots\dots\dots, y = \dots\dots\dots \\ x &= \dots\dots\dots, y = \dots\dots\dots [5] \end{aligned}$$

23 $\mathbf{a} = \begin{pmatrix} 2 \\ -4 \end{pmatrix}$ $\mathbf{b} = \begin{pmatrix} 3 \\ 6 \end{pmatrix}$

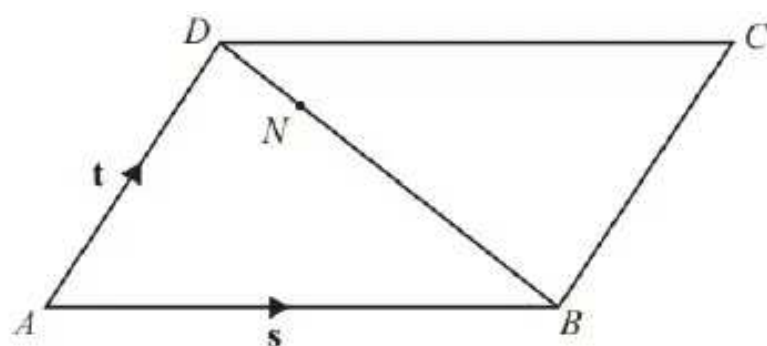
Find

(a) $3\mathbf{a}$, () [1]

(b) $2\mathbf{b}$, () [1]

(c) $4\mathbf{a} + \mathbf{b}$ () [2]

24

NOT TO
SCALE

$ABCD$ is a parallelogram.

N is the point on BD such that $BN : ND = 4 : 1$.

$\vec{AB} = \mathbf{s}$ and $\vec{AD} = \mathbf{t}$.

Find, in terms of \mathbf{s} and \mathbf{t} , an expression in its simplest form for

(a) \vec{BD} ,

$$\vec{BD} = \dots\dots\dots [1]$$

(b) \vec{CN} .

$$\vec{CN} = \dots\dots\dots [3]$$

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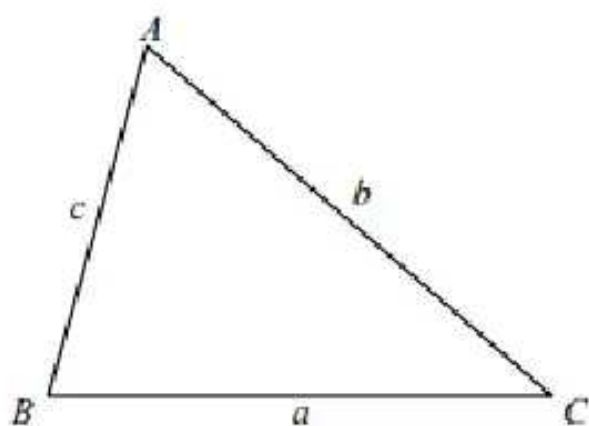
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For the triangle shown,



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$$\text{Area} = \frac{1}{2}ab \sin C$$

Calculators must **not** be used in this paper.

- 1 Work out $\frac{4}{9} \times \frac{27}{20}$.

Give your answer as a fraction in its simplest form.

$$\frac{\cancel{4}^2}{9} \times \frac{\cancel{27}^3}{\cancel{20}_5} = \frac{3}{5}$$

..... $\frac{3}{5}$ [1]

- 2 Write down the order of rotational symmetry of a parallelogram.



..... 2 [1]

- 3 Convert 22400 cm^2 into m^2

$$\begin{aligned} 1 \text{ cm} &= 0.01 \text{ m} \\ 1 \text{ cm}^2 &= (0.01)^2 = 0.0001 \text{ m}^2 \\ \times 22400 \quad 22400 \text{ cm}^2 &= \underline{2.24 \text{ m}^2} \quad \times 22400 \end{aligned}$$

..... 2.24 m^2 [2]

- 4 John has a biased 6-sided die.

Number	1	2	3	4	5	6
Probability	0.10	0.05	0.25	0.20	0.30	0.10

John rolls the die

$$1 - 0.10 - 0.25 - 0.20 - 0.30 - 0.10 = 0.05$$

Calculate the probability that it lands on a prime number.

2, 3 or 5

$$0.05 + 0.25 + 0.30 = \underline{0.60}$$

..... 0.6 [3]

- 5 Find the value of $343^{\frac{2}{3}}$.

$$\begin{aligned} &(\sqrt[3]{343})^2 \\ &= 7^2 = 49 \end{aligned}$$

..... 49 [2]

- 6 Find the Highest Common Factor (HCF) of 51 and 119

$$\begin{array}{c} 51 \\ \swarrow \quad \searrow \\ 3 \quad 17 \end{array}$$

$$\begin{array}{c} 119 \\ \swarrow \quad \searrow \\ 7 \quad 17 \end{array}$$

$$51 = 3 \times 17$$

$$119 = 7 \times 17$$

$$\therefore \text{HCF} = 17.$$

.....17 [2]

- 7 y is inversely proportional to $(x + 1)^3$

When $x = 1$, $y = 0.5$

- (a) Calculate the value of y when $x = 3$.

$$y \propto \frac{1}{(x+1)^3}$$

$$y = \frac{k}{(x+1)^3}$$

$$0.5 = \frac{k}{(1+1)^3} = \frac{k}{2^3} = \frac{k}{8}$$

$$\therefore k = 4$$

$$y = \frac{4}{(x+1)^3}$$

$$y = \frac{4}{(3+1)^3} = \frac{4}{4^3} = \frac{4}{64} = \frac{1}{16}$$

$y = \frac{1}{16}$ [4]

- (b) Find the value of x when $y = \frac{1}{16}$.

$$\frac{1}{16} = \frac{4}{(x+1)^3}$$

$$(x+1)^3 = \frac{4}{\frac{1}{16}} = 4 \times 16 = 64$$

$$\therefore x+1 = 4$$

$$\Rightarrow x = 3.$$

$x = 3$ [3]

- 8 (a) Simplify.

$$\sqrt{8} + \sqrt{50}$$

$$\sqrt{8} = 2\sqrt{2}$$

$$\sqrt{50} = 5\sqrt{2}$$

$$2\sqrt{2} + 5\sqrt{2} = 7\sqrt{2}$$

5

$$7\sqrt{2}$$

..... [2]

(b) Rationalise the denominator.

$$\frac{2}{\sqrt{3}+1}$$

$$= \frac{2}{\sqrt{3}+1} \times \frac{\sqrt{3}-1}{\sqrt{3}-1}$$

$$= \frac{2(\sqrt{3}-1)}{(\sqrt{3}+1)(\sqrt{3}-1)} = \frac{2(\sqrt{3}-1)}{3-1}$$

$$= \frac{2(\sqrt{3}-1)}{2} = \sqrt{3}-1$$

..... [2]

9 Without using a calculator, work out $3\frac{2}{7} + \frac{4}{9}$.

You must show all your working and give your answer as a mixed number in its simplest form.

$$3\frac{2}{7} = \frac{23}{7}$$

$$\frac{23}{7} + \frac{4}{9}$$

$$= \frac{23 \times 9}{63} + \frac{4 \times 7}{63}$$

$$= \frac{235}{63}$$

$$= 3\frac{46}{63}$$

$$3\frac{46}{63}$$

..... [3]

10

The diagram shows the speed–time graph for part of the journey of a car.



The car starts from rest and accelerates at a uniform rate for 15 seconds before reaching a constant speed of 30 m/s.

- (a) Calculate the acceleration for the first 15 seconds.

$$a = \frac{\Delta s}{\Delta t} = \frac{30}{15} = 2 \text{ m/s}^2$$

..... 2 m/s² [1]

- (b) After T minutes, the total distance travelled is ^{35.775}~~45~~ kilometres.
60T seconds. 35775 m

Find the value of T.

Distance = area under the curve.

$$35775 = \frac{1}{2}(30)(15) + 30(60T - 15)$$

$$35775 = 225 + 1800T - 450$$

$$1800T = 36000$$

$$T = 20$$

T = 20 min [4]

11

The scale of a map is 1 : 2000.

The area of a road is 400m².

Calculate the area of the road on the map, giving your answer in cm².

Linear SF: 1 : 2000

Area SF: 1 : 200² ⇒ 1 : 40000

$x = \frac{1}{100} \text{ m}^2 = 0.01 \text{ m}^2$

$1 \text{ m}^2 = 10000 \text{ cm}^2$

∴ $0.01 \text{ m}^2 = 100 \text{ cm}^2$

..... 100 cm² [3]

12

- (a) Dina invests \$2000 in an account that pays simple interest at a rate of $r\%$ per year.

At the end of 3 years, the account has earned \$300 in **interest**.

Calculate the value of r .

$$\frac{Prt}{100} = 300$$

$$\frac{2000 \times r \times 3}{100} = 300$$

$$20 \times r \times 3 = 300$$

$$60r = 300$$

$$\therefore r = 5$$

$r = 5$ [3]

(b)

- (i) Hence, or otherwise, calculate the total value of her investment after 6 years.

At the end of 6 years, interest gained is:
 $2 \times \$300 = \600 .

$$\therefore \text{Total value} = \$2000 + \$600$$

$$= \$2600$$

\$2600 [2]

- (ii) Marcus invests \$2500 in a bank which pays simple interest at a rate of 2% per year.

At the end of 6 years, whose investment is most valuable? Give a comparison to justify your answer.

$$\text{Marcus: } 2500 + \frac{2500 \times 2 \times 6}{100} = 2500 + 300$$

$$= \$2800$$

Marcus' investment is most valuable. He has made \$2800, whereas Dina has made \$2600. [2]

13

A is the point $(5, -5)$ and B is the point $(9, 3)$.

(a) Find the coordinates of the midpoint of AB .

$$\begin{aligned} & \left(\frac{5+9}{2}, \frac{-5+3}{2} \right) \\ \hookrightarrow & \left(\frac{14}{2}, \frac{-2}{2} \right) \\ \hookrightarrow & (7, -1) \end{aligned}$$

(.....7.....,-1.....) [2]

(b) Find the length of AB .

Give your answer in exact form.

$$\begin{aligned} & \sqrt{(9-5)^2 + (3-(-5))^2} \\ &= \sqrt{4^2 + 8^2} \\ &= \sqrt{16 + 64} \\ &= \sqrt{80} \\ &= 4\sqrt{5} \end{aligned}$$

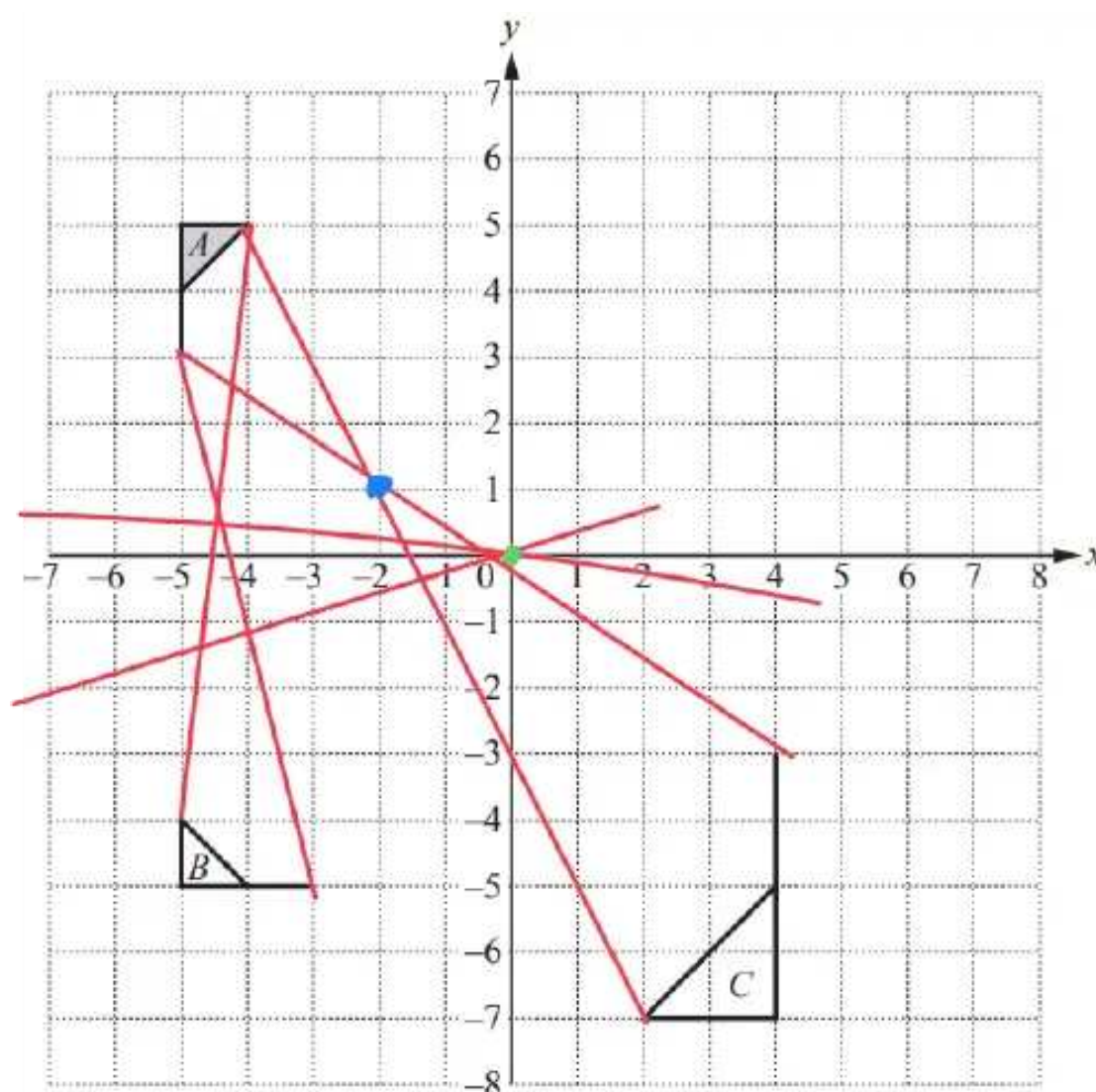
.....4\sqrt{5}..... [3]

(c) Write down the gradient of a line that is perpendicular to the line AB

$$\begin{aligned} m_{AB} &= \frac{3-(-5)}{9-5} = \frac{8}{4} = 2 \\ \therefore m_{\perp} &= -\frac{1}{2} \end{aligned}$$

.....-\frac{1}{2}..... [2]

14



(a) Describe fully the **single** transformation that maps

(i) Flag B onto Flag A,

Rotation, centre $(0, 0)$; 90° anticlockwise.

..... [3]

(ii) Flag A onto Flag C,

Enlargement, centre $(-2, 1)$;
scale factor -2 .

..... [3]

15 Simplify: $\frac{2x^2+5x-12}{4x^2-9}$

$$\frac{(2x-3)(x+4)}{(2x-3)(2x+3)} = \frac{x+4}{2x+3}$$

$$\frac{x+4}{2x+3}$$

.....[4]

16

(a) x is an integer.

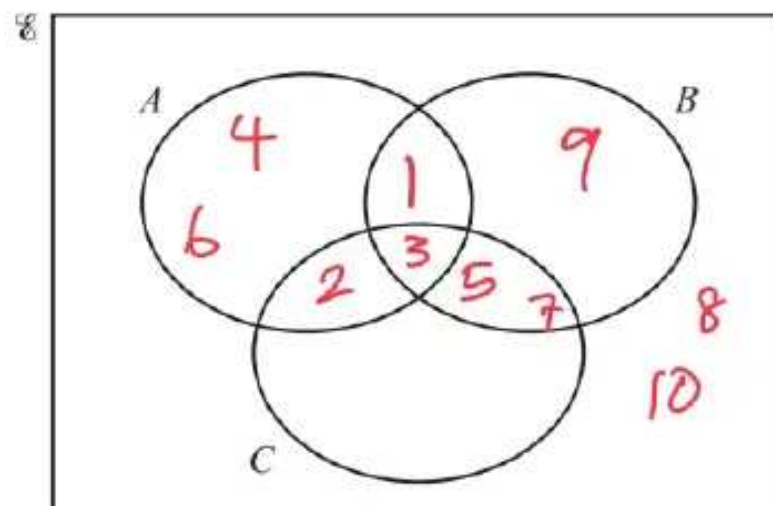
$$\mathcal{U} = \{x: 1 \leq x \leq 10\}$$

$$A = \{x: x \text{ is a factor of } 12\}$$

$$B = \{x: x \text{ is an odd number}\}$$

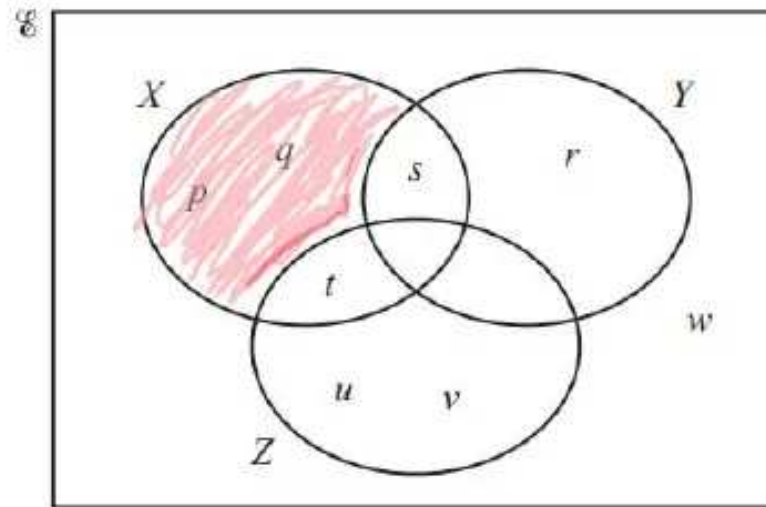
$$C = \{x: x \text{ is a prime number}\}$$

(i) Complete the Venn diagram to show this information.



[3]

(b)



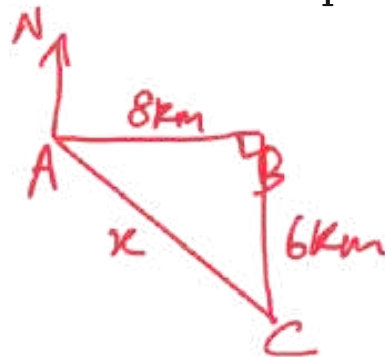
(i) Use set notation to complete the statement.

 $\{u, v\} \subset Z$ [1]
(ii) Shade $X \cap (Z \cup Y)'$.

[1]

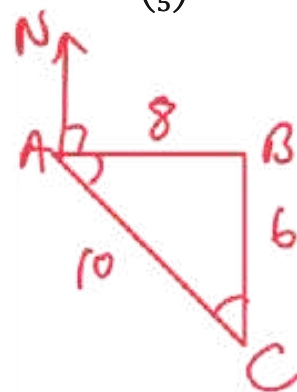
- 17 A plane leaves airport A and flies 8 km on a bearing of 090° to reach point B. From point B, it changes direction and flies 6 km on a bearing of 180° to reach point C.

(a) Calculate the distance from point A to point C.



$$\begin{aligned} x^2 &= 8^2 + 6^2 \\ x &= \sqrt{8^2 + 6^2} \\ x &= \sqrt{64 + 36} = \sqrt{100} \\ \therefore x &= 10 \text{ km} \end{aligned}$$

.....10 km [3]

(b) Given that $\sin^{-1}\left(\frac{4}{5}\right) = 53.1^\circ$, determine the bearing of point C from point A.

$$\begin{aligned} \sin \angle BCA &= \frac{8}{10} = \frac{4}{5} \\ \sin^{-1}\left(\frac{4}{5}\right) &= 53.1^\circ \Rightarrow \angle BCA = 53.1^\circ \\ \angle BAC &= 180 - 90 - 53.1^\circ = 36.9^\circ \\ \therefore 090^\circ + 36.9^\circ &= 126.9^\circ \end{aligned}$$

.....126.9° [3]

18 Find the n th term of each of the following sequences:

(a) 2, 5, 8, 11, 14, ...
 $+3 +3 +3 \dots$

$$3n - 1$$

0th term,
i.e., the term
before the first.

..... $3n - 1$ [2]

(b) -2, 2, 8, 16, 26, ...

$+4 +6 +8 +10$
 $+2 +2 +2$
 $\div 2 \rightarrow n^2 + bn + c$

$n^2 + bn + c$	-2, 2, 8, 16...
$- n^2$	1, 4, 9, 16...
$bn + c$	-3, -2, -1, 0
	$+1 +1 +1$

$$\therefore bn + c = n - 4$$

$$\therefore n^2 + n - 4$$

..... $n^2 + n - 4$ [3]

19 Calculate the area of a semicircle with diameter 10cm.

Give your answer in exact form.



$$r = \frac{d}{2} = \frac{10}{2} = 5 \text{ cm}$$

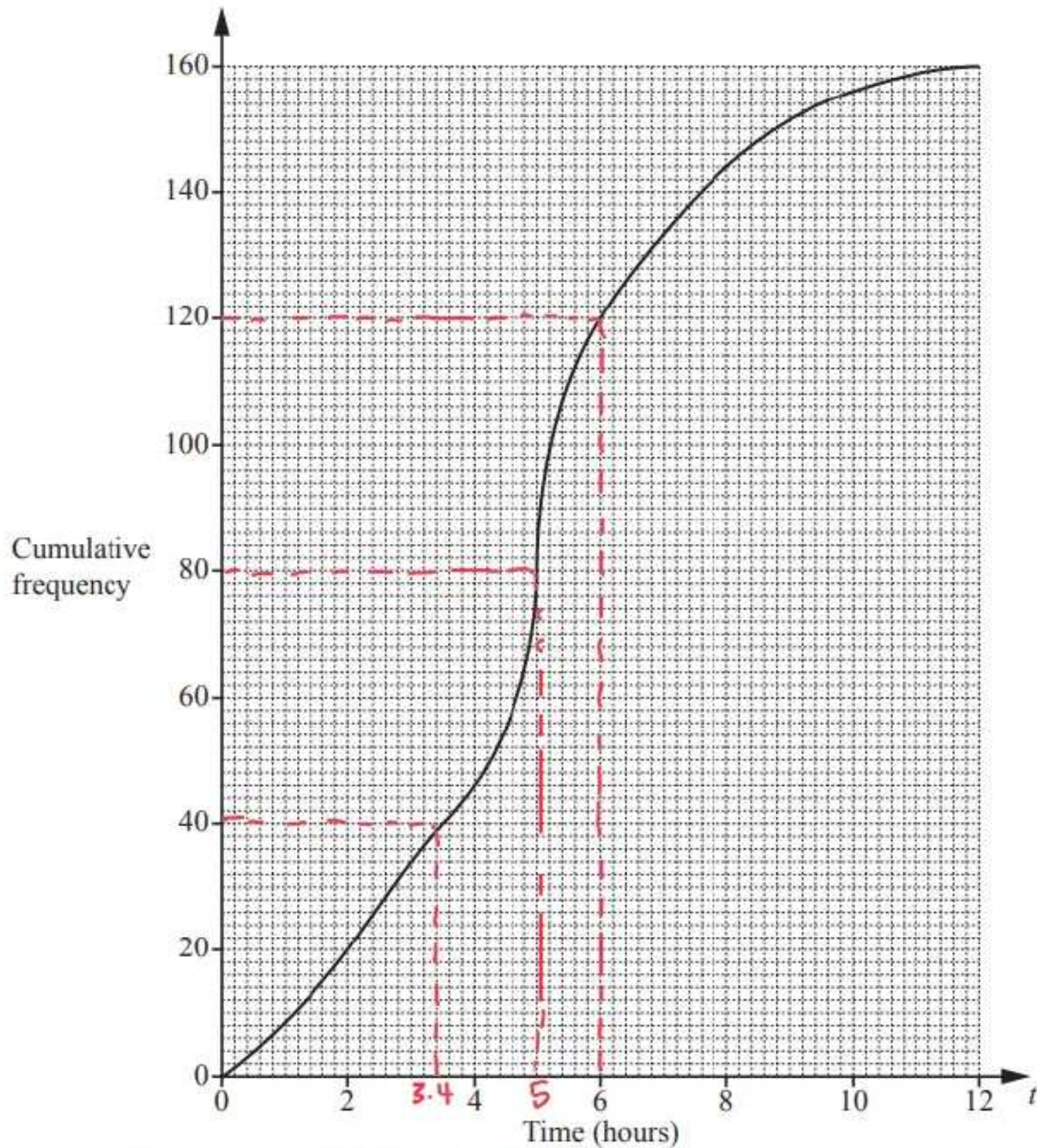
$$A = \frac{\pi r^2}{2} = \frac{\pi (5)^2}{2}$$

$$= \frac{25\pi}{2} \text{ cm}^2$$

..... $\frac{25\pi}{2} \text{ cm}^2$ [3]

20

160 students record the amount of time, t hours, they each spend playing computer games in a week. This information is shown in the cumulative frequency diagram.



(a) Use the diagram to find an estimate of

(i) the median,

.....5 hours [1]

(ii) the interquartile range,

$$\begin{aligned} \text{IQR} &= \text{UQ} - \text{LQ} \\ &= 6 - 3.4 \\ &= 2.6 \text{ hrs.} \end{aligned}$$

.....2.6 hours [2]

(b) Use the diagram to complete this frequency table.

Time (t hours)	$0 < t \leq 2$	$2 < t \leq 4$	$4 < t \leq 6$	$6 < t \leq 8$	$8 < t \leq 10$	$10 < t \leq 12$
Frequency	20	26	74	24	12	4

[2]

21

(a) Write $x^2 - 8x + 12$ in the form $(x - a)^2 + b$.

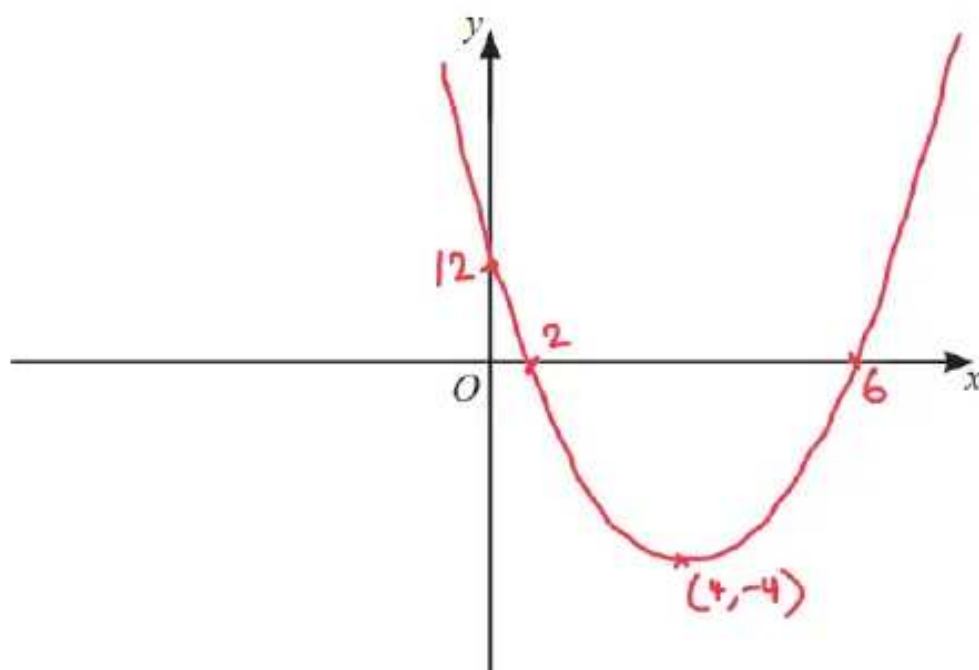
$$\begin{aligned} (x-4)^2 - 16 + 12 \\ = (x-4)^2 - 4 \end{aligned}$$

$$(x-4)^2 - 4 \dots\dots\dots [2]$$

(b) Hence, write down the coordinates of the turning point of the graph of $y = x^2 - 8x + 12$.

$$(\dots\dots\dots 4 \dots\dots\dots, \dots\dots\dots -4 \dots\dots\dots) [1]$$

(c)



On the diagram, sketch the graph of $y = x^2 - 8x + 12$.

[3]

- 22 Solve the simultaneous equations.
You must show all your working.

$$\begin{aligned}
 2x^2 + 3y &= -8 \\
 \frac{4}{3} + y &= -2x \Rightarrow y = -2x - \frac{4}{3} \\
 2x^2 + 3\left(-2x - \frac{4}{3}\right) &= -8 \\
 2x^2 - 6x - 4 &= -8 \\
 2x^2 - 6x + 4 &= 0 \\
 x^2 - 3x + 2 &= 0 \\
 (x-2)(x-1) &= 0 \\
 x=2 & \quad x=1 \\
 \hookrightarrow y = -2(2) - \frac{4}{3} & \quad \hookrightarrow y = -2(1) - \frac{2}{3} \\
 y = -\frac{16}{3} & \quad y = -\frac{10}{3}
 \end{aligned}$$

$$x = \dots\dots\dots 1 \dots\dots\dots, y = \dots\dots\dots -\frac{10}{3} \dots\dots\dots$$

$$x = \dots\dots\dots 2 \dots\dots\dots, y = \dots\dots\dots -\frac{16}{3} \dots\dots\dots [5]$$

23 $\mathbf{a} = \begin{pmatrix} 2 \\ -4 \end{pmatrix}$ $\mathbf{b} = \begin{pmatrix} 3 \\ 6 \end{pmatrix}$

Find

(a) $3\mathbf{a}$,

$$\begin{pmatrix} 6 \\ -12 \end{pmatrix} [1]$$

(b) $2\mathbf{b}$,

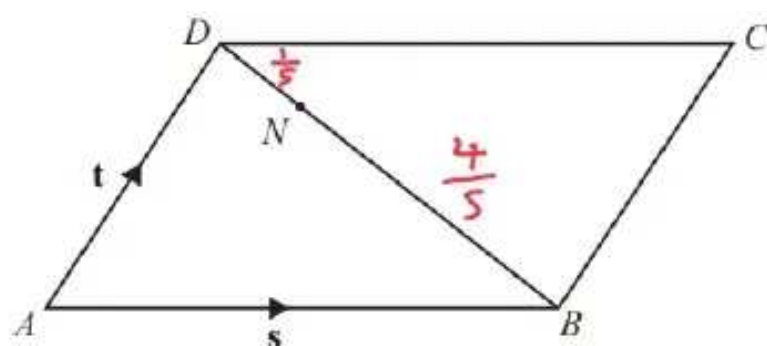
$$\begin{pmatrix} 6 \\ 12 \end{pmatrix} [1]$$

(c) $4\mathbf{a} + \mathbf{b}$

$$\begin{aligned}
 &\begin{pmatrix} 8 \\ -16 \end{pmatrix} + \begin{pmatrix} 3 \\ 6 \end{pmatrix} \\
 &\hookrightarrow \begin{pmatrix} 11 \\ -10 \end{pmatrix}
 \end{aligned}$$

$$\begin{pmatrix} 11 \\ -10 \end{pmatrix} [2]$$

24



$ABCD$ is a parallelogram.

N is the point on BD such that $BN : ND = 4 : 1$.

$\vec{AB} = \mathbf{s}$ and $\vec{AD} = \mathbf{t}$.

Find, in terms of \mathbf{s} and \mathbf{t} , an expression in its simplest form for

(a) \vec{BD} ,

$$\vec{BD} = \underline{\underline{\mathbf{t} - \mathbf{s}}} \quad [1]$$

(b) \vec{CN} .

$$\begin{aligned} \vec{CN} &= \vec{CB} + \frac{4}{5} \vec{BD} \\ &= -\underline{\underline{\mathbf{t}}} + \frac{4}{5} (\underline{\underline{\mathbf{t}}} - \underline{\underline{\mathbf{s}}}) \\ \therefore \vec{CN} &= -\underline{\underline{\mathbf{t}}} + \frac{4}{5} \underline{\underline{\mathbf{t}}} - \frac{4}{5} \underline{\underline{\mathbf{s}}} \\ &= -\frac{1}{5} \underline{\underline{\mathbf{t}}} - \frac{4}{5} \underline{\underline{\mathbf{s}}} \end{aligned}$$

$$\vec{CN} = \underline{\underline{-\frac{1}{5} \mathbf{t} - \frac{4}{5} \mathbf{s}}} \quad [3]$$



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MATHEMATICS

0580/41

Paper 4 Calculator (Extended)

February/March 2025

2 hours

You must answer on the question paper.

You will need: Geometrical instruments

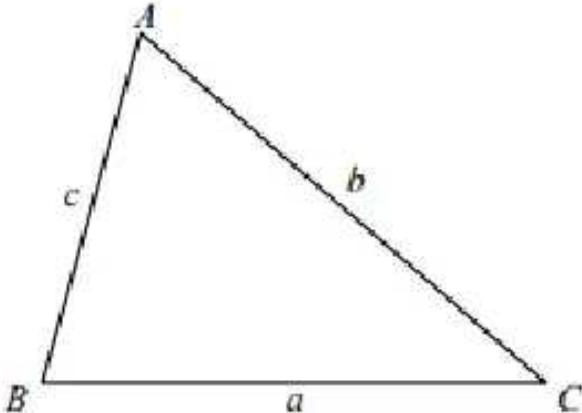
INSTRUCTIONS

- Answer **all** questions.
- Use a black or dark blue pen. You may use an HB pencil for any diagrams or graphs.
- Write your name, centre number and candidate number in the boxes at the top of the page.
- Write your answer to each question in the space provided.
- Do **not** use an erasable pen or correction fluid.
- Do **not** write on any bar codes.
- You should use a scientific calculator where appropriate.
- You may use tracing paper
- You must show all necessary working clearly.
- Give non-exact numerical answers correct to 3 significant figures, or 1 decimal place for angles in degrees, unless a different level of accuracy is specified in the question.
- For π , use either your calculator value or 3.142.

INFORMATION

- The total mark for this paper is 100.
- The number of marks for each question or part question is shown in brackets [].
For extra guidance, use the [All of iGCSE Maths Playlist](#)

List of formulas

Area, A , of triangle, base b , height h .	$A = \frac{1}{2}bh$
Area, A , of circle of radius r .	$A = \pi r^2$
Circumference, C , of circle of radius r .	$C = 2\pi r$
Curved surface area, A , of cylinder of radius r , height h .	$A = 2\pi rh$
Curved surface area, A , of cone of radius r , sloping edge l .	$A = \pi rl$
Surface area, A , of sphere of radius r .	$A = 4\pi r^2$
Volume, V , of prism, cross-sectional area A , length l .	$V = Al$
Volume, V , of pyramid, base area A , height h .	$V = \frac{1}{3}Ah$
Volume, V , of cylinder of radius r , height h .	$V = \pi r^2 h$
Volume, V , of cone of radius r , height h .	$V = \frac{1}{3}\pi r^2 h$
Volume, V , of sphere of radius r .	$V = \frac{4}{3}\pi r^3$
For the equation $ax^2 + bx + c = 0$, where $a \neq 0$,	$x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$
For the triangle shown,	
	$\frac{a}{\sin A} = \frac{b}{\sin B} = \frac{c}{\sin C}$
	$a^2 = b^2 + c^2 - 2bc \cos A$
	$\text{Area} = \frac{1}{2}ab \sin C$

1 Martin receives \$800 from his grandmother.

- (a) He decides to spend \$150 and to divide the remaining \$650 in the ratio savings:holiday = 9:4.
Calculate the amount of his savings.

\$..... [2]

- (b) i He uses 80% of the \$150 to buy some clothes.
Calculate the cost of the clothes.

$$\frac{80}{100} \times 150 = 120$$

\$..... [2]

- ii The money remaining from the \$150 is 37.5% of the cost of a day trip to Athens. Calculate the cost of the trip.

$$0.375 \times x = 30 \quad x = 80$$

$$x = \frac{30}{0.375}$$

\$80..... [2]

- (c) i Martin invests \$400 of his savings for 2 years at 5% per annum compound interest.
Calculate the amount he has at the end of the 2 years.

\$..... [2]

- ii Martin's sister also invests \$400, at $r\%$ per annum simple interest.
At the end of 2 years, she has exactly the same amount as Marcus.

Calculate the value of r .

$r =$ [2]

2

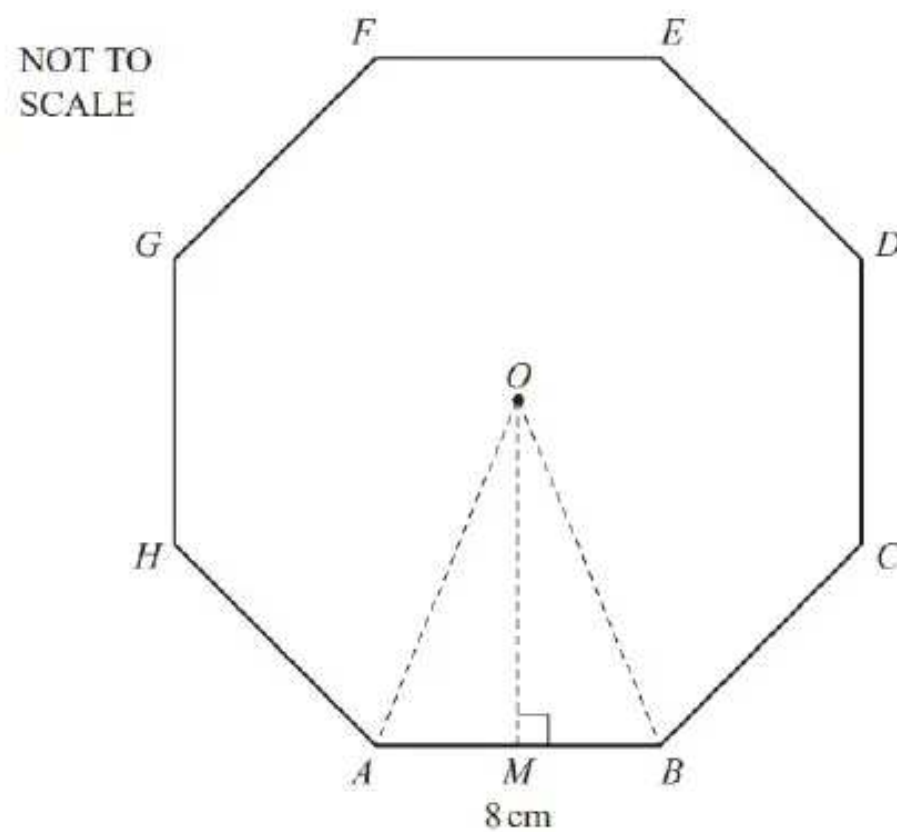
- (a) Write down the name of a polygon with 8 sides.

..... [1]

- (b) Find the size of the interior angle of a regular polygon with 8 sides.

..... [2]

- (c) A regular 8-sided polygon, centre O , and side 8 cm, is shown below.
 M is the mid-point of the side AB .



- (i) Show that $OM = 9.66$ cm correct to 3 significant figures.

[3]

(ii) Calculate the area of the polygon.

.....cm² [3]

- (d)** The polygon forms the cross-section of a box.
The box is a prism of height 12cm.

Calculate the volume of the box.

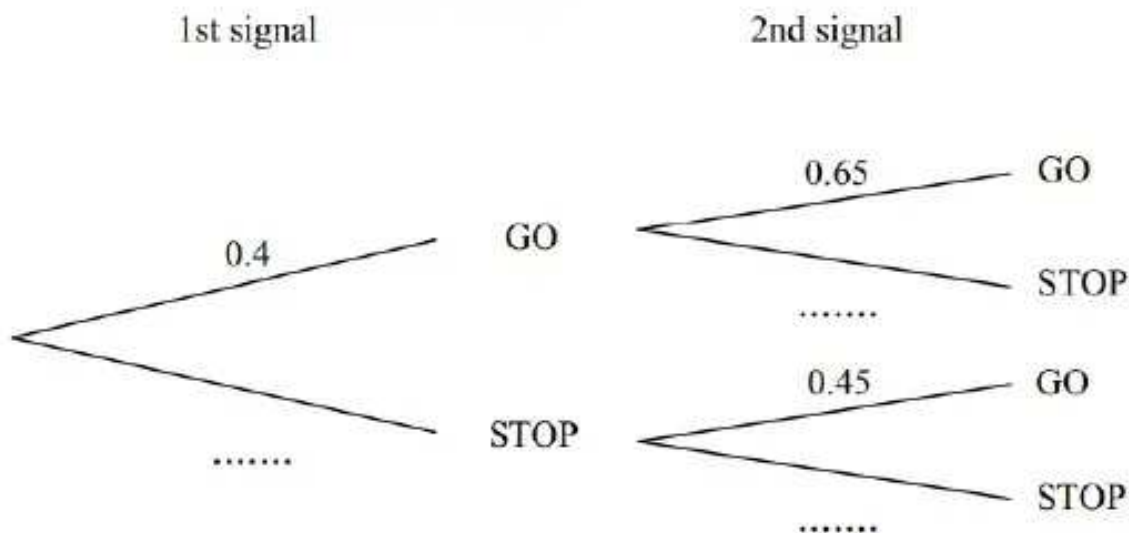
.....cm³ [1]

- (e)** The box contains 100 toffees in the shape of spheres, each with a radius of 2cm.
Calculate the percentage of the volume of the box **not** filled by the toffees.

.....cm³ [5]

- 3** There are 2 sets of road signals on the direct 12 kilometre route from Liverpool to Manchester. The signals say either “GO” or “STOP”.

(a) Complete the tree diagram for a driver travelling along this route.



[3]

- (b)** Find the probability that a car driver

i finds both signals are “GO”,

.....[2]

ii finds exactly one of the signals is “GO”,

.....[3]

iii does not find two “STOP” signals

.....[2]

- (c) With no stops, Damon completes the 12km journey at an average speed of 40 kilometres per hour.

i find the time taken in minutes for this journey.

.....mins [1]

ii When Damon has to stop at a signal, it adds 3 minutes to this journey time. Calculate his average speed, in kilometres per hour, if he stops at both road signals.

.....kph [2]

- (d) Elsa takes a different route from Liverpool to Manchester. This route is 15 kilometres and there are no road signals. Elsa's average speed for this journey is 40 kilometres per hour. Find

i the time taken in minutes for this journey,

(e)

.....mins [1]

i the probability that Damon takes more time than this on his 12 kilometre journey.

..... [2]

- 4 $x = \sqrt[3]{b^3 c}$
(a) Find the value of x when $b = 4$ and $c = 9$.

$x =$ [2]

(b) Rearrange the formula to write c in terms of x and b .

$c =$ [2]

5 Solve.
(a) $2(3 - 8x) = 54$

..... [2]

(b) $\frac{1}{y} = \frac{1}{y+3}^2$

$y =$ or $y =$ [3]

6

200 students were asked how many hours they exercise each week.
The table shows the results.

Time (t hours)	$0 < t \leq 5$	$5 < t \leq 10$	$10 < t \leq 15$	$15 < t \leq 20$	$20 < t \leq 25$	$25 < t \leq 30$	$30 < t \leq 35$	$35 < t \leq 40$
Number of students	12	15	23	30	40	35	25	20

(a) Calculate an estimate of the mean.

.....h[4]

9

(b) Use the information in the table above to complete the cumulative frequency table.

Time (t hours)	$t \leq 5$	$t \leq 10$	$t \leq 15$	$t \leq 20$	$t \leq 25$	$t \leq 30$	$t \leq 35$	$t \leq 40$
Cumulative frequency	12	27	50	80	120			200

[1]

7 This question is about sequences.

(a) Find the 22nd term in the following sequence:

-2, 3, 8, 13, ...

..... [3]

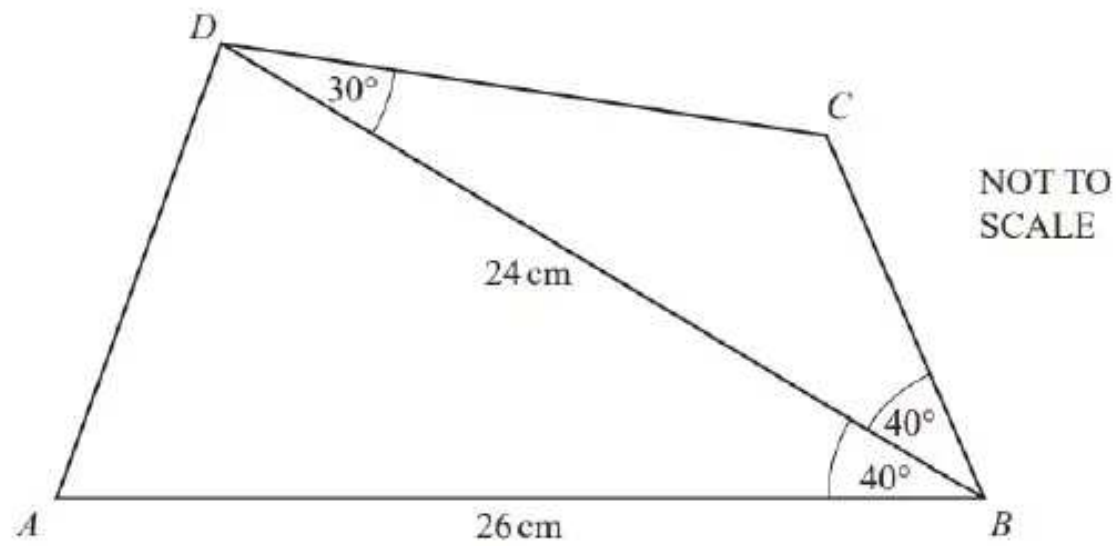
(b) T_n is defined by the terms:

0.5, 1, 2, 4, ...

What is the smallest value of n for which T_n exceeds 875?

$n =$ [4]

8



$ABCD$ is a quadrilateral and BD is a diagonal.

$AB = 26\text{ cm}$, $BD = 24\text{ cm}$, angle $ABD = 40^\circ$, angle $CBD = 40^\circ$ and angle $CDB = 30^\circ$.

(a) Calculate the area of triangle ABD .

..... cm^2 [2]

(b) Calculate the length of AD .

..... cm [4]

(c) Calculate the length of BC .

..... cm [4]

(d) Calculate the shortest distance from the point C to the line BD .

..... cm [2]

9

$$f(x) = x^2 - 4x + 3 \text{ and } g(x) = 2x - 3$$

(a) Solve $f(x) = 0$

(b) Find $g^{-1}(x)$

..... [2]

..... [2]

(c) Solve $f(x) = g(x)$, giving each of your answers correct to 2 decimal places.

$x = \dots\dots\dots$ or $x = \dots\dots\dots$ [3]

(d) Find $gf(-2x)$, simplifying your expression.

..... [4]

(e) Hence, or otherwise, find the value of $gf(4)$

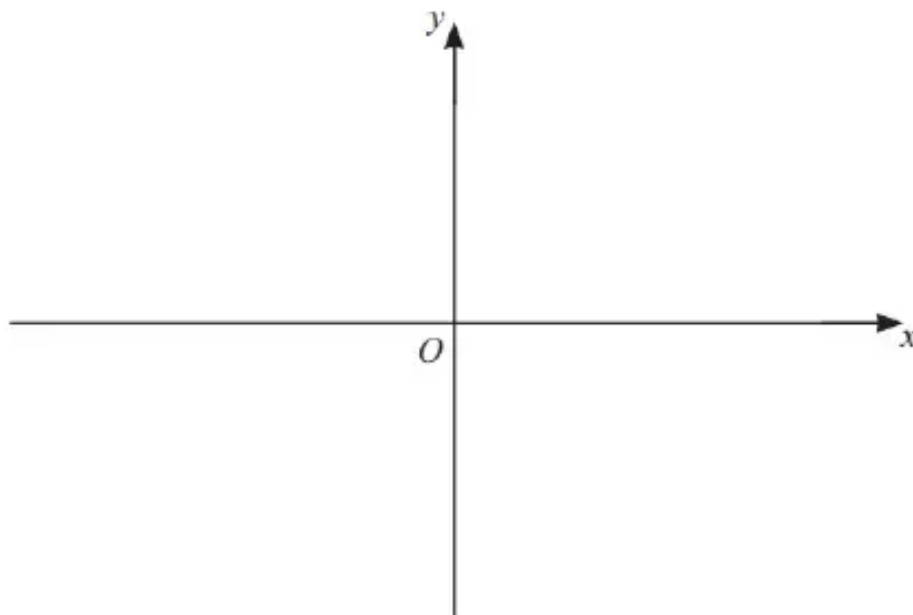
..... [2]

10

(a) Solve the equation $\sin x = 0.357$ for $0^\circ \leq x \leq 360^\circ$.

$x = \dots\dots\dots$ or $x = \dots\dots\dots$ [2]

(b) Sketch the curve $y = x^3 - 4x$.



[3]

13

(c) A curve has equation $y = x^3 + px^2 + qx + r$

The stationary points of the curve occur when $x = 1$ and $x = -2$

Given that the curve passes through the point $(0, 4)$, work out the values of p , q and r .

$p = \dots\dots\dots, q = \dots\dots\dots, r = \dots\dots\dots$ [8]

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MATHEMATICS

0580/41

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$$A = 2\pi rh$$

Curved surface area, A , of cone of radius r , sloping edge l .

$$A = \pi rl$$

Surface area, A , of sphere of radius r .

$$A = 4\pi r^2$$

Volume, V , of prism, cross-sectional area A , length l .

$$V = Al$$

Volume, V , of pyramid, base area A , height h .

$$V = \frac{1}{3}Ah$$

Volume, V , of cylinder of radius r , height h .

$$V = \pi r^2 h$$

Volume, V , of cone of radius r , height h .

$$V = \frac{1}{3}\pi r^2 h$$

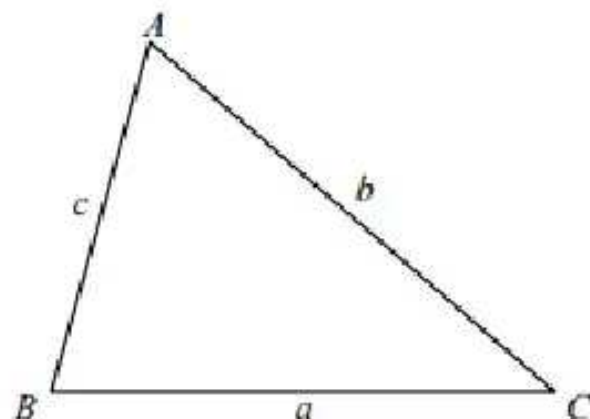
Volume, V , of sphere of radius r .

$$V = \frac{4}{3}\pi r^3$$

For the equation $ax^2 + bx + c = 0$, where $a \neq 0$,

$$x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$$

For the triangle shown,



$$\frac{a}{\sin A} = \frac{b}{\sin B} = \frac{c}{\sin C}$$

$$a^2 = b^2 + c^2 - 2bc \cos A$$

$$\text{Area} = \frac{1}{2}ab \sin C$$

1 Martin receives \$800 from his grandmother.

- (a) He decides to spend \$150 and to divide the remaining \$650 in the ratio savings:holiday = 9:4. Calculate the amount of his savings.

$$\begin{aligned}\frac{9}{9+4} \times \$650 \\ &= \frac{9}{13} \times 650 \\ &= \$450\end{aligned}$$

\$.....450..... [2]

(b)

- i He uses 80% of the \$150 to buy some clothes. Calculate the cost of the clothes.

$$\begin{aligned}0.8 \times 150 \\ &= \$120\end{aligned}$$

\$.....120..... [2]

- ii The money remaining from the \$150 is 37.5% of the cost of a day trip to Athens. Calculate the cost of the trip.

$$\begin{aligned}\$150 - \$120 &= \$30. \\ 0.375x &= 30 \\ \therefore x &= \frac{30}{0.375} = \$80\end{aligned}$$

\$.....80..... [2]

(c)

- i Martin invests \$400 of his savings for 2 years at 5% per annum compound interest. Calculate the amount he has at the end of the 2 years.

$$\begin{aligned}400 \left(1 + \frac{5}{100}\right)^2 \\ &= \$441\end{aligned}$$

\$.....441..... [2]

- ii Martin's sister also invests \$400, at $r\%$ per annum simple interest. At the end of 2 years, she has exactly the same amount as Marcus.

Calculate the value of r .

$$\begin{aligned}400 + \frac{400 \times r \times 2}{100} &= 441 \\ \frac{800r}{100} &= 41 \\ 8r &= 41 \\ \therefore r &= 5.125\end{aligned}$$

$r =$5.125..... [2]

2

- (a) Write down the name of a polygon with 8 sides.

Octagon..... [1]

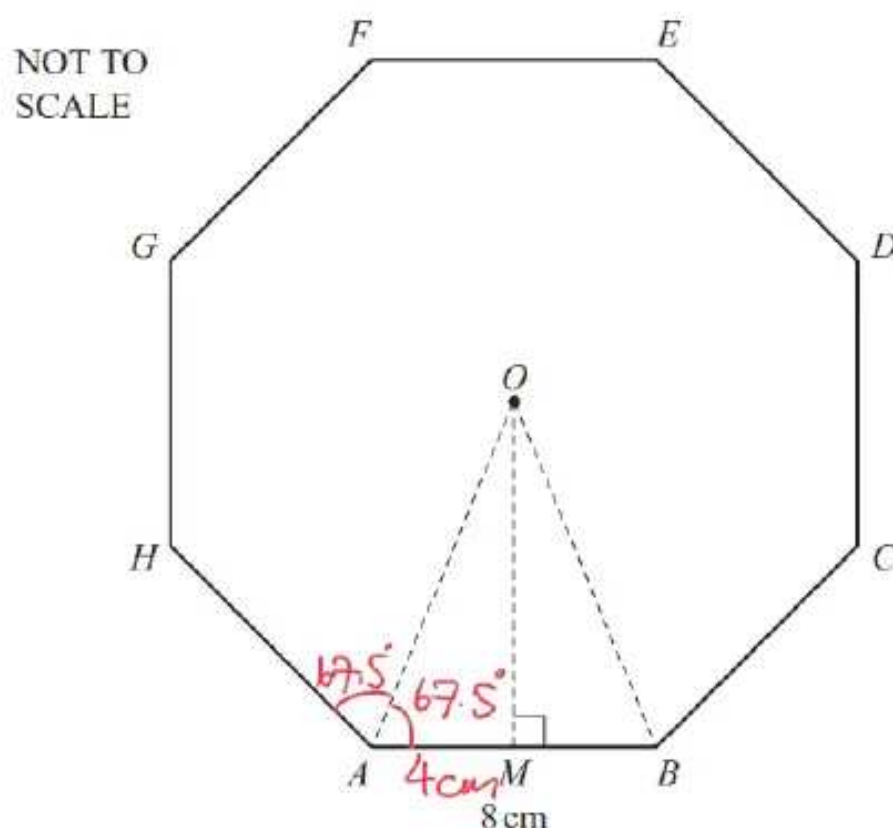
- (b) Find the size of the interior angle of a regular polygon with 8 sides.

$$\frac{180(n-2)}{n} = \frac{180(8-2)}{8}$$

$$= 135^\circ$$

135..... [2]

- (c) A regular 8-sided polygon, centre O , and side 8 cm, is shown below.
 M is the mid-point of the side AB .



- (i) Show that $OM = 9.66$ cm correct to 3 significant figures.

$$\tan 67.5 = \frac{OM}{4}$$

$$OM = 4 \tan 67.5$$

$$\therefore OM = 9.656...$$

$$= 9.66 \text{ cm (3 s.f.)}$$

[3]

(ii) Calculate the area of the polygon.

Area of $\triangle AOB$.

$$8 \times \left[\frac{1}{2} \times 8 \times 9.66 \right]$$

$$= 309.01 \dots$$

$$= 309 \text{ cm}^2 \text{ (3 s.f.)}$$

.....309 cm² [3]

(d) The polygon forms the cross-section of a box.
The box is a prism of height 12cm.

Calculate the volume of the box.

$$309 \times 12 = 3708$$

$$= 3710 \text{ cm}^3 \text{ (3 s.f.)}$$

.....3710 cm³ [1]

(e) The box contains 100 toffees in the shape of spheres, each with a radius of 2cm.
Calculate the percentage of the volume of the box not filled by the toffees.

$$100 \times \left[\frac{4}{3} \pi \times (2)^3 \right]$$

$$= \frac{3200}{3} \pi$$

$$V_{\text{not filled}} = 3710 - \frac{3200\pi}{3}$$

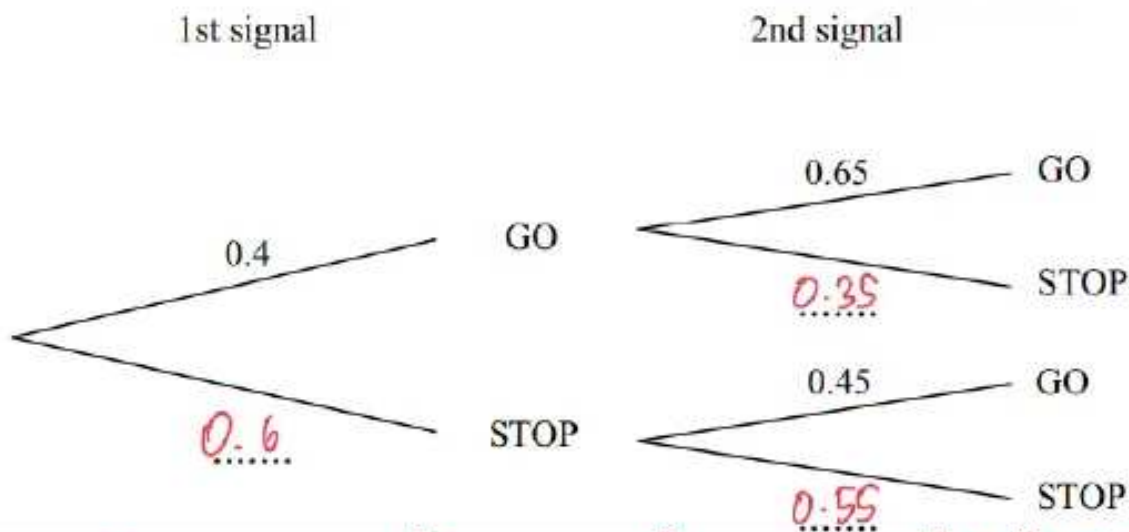
$$\% = \frac{3710 - \frac{3200\pi}{3}}{3710} \times 100$$

$$= 9.68\% \text{ (3 s.f.)}$$

.....9.68 % [5]

- 3 There are 2 sets of road signals on the direct 12 kilometre route from Liverpool to Manchester. The signals say either “GO” or “STOP”.

(a) Complete the tree diagram for a driver travelling along this route.



[3]

- (b) Find the probability that a car driver

i finds both signals are “GO”,

$$0.4 \times 0.65 = 0.26$$

0.26

.....[2]

ii finds exactly one of the signals is “GO”,

$$(0.4 \times 0.35) + (0.6 \times 0.45) = 0.4$$

0.4

.....[3]

iii does not find two “STOP” signals

$$1 - (0.6 \times 0.55) = 0.67$$

0.67

.....[2]

- (c) With no stops, Damon completes the 12km journey at an average speed of 40 kilometres per hour.

i find the time taken in minutes for this journey.

$$\frac{12}{40} \times 60 = 18 \text{ mins}$$

.....18 mins [1]

ii When Damon has to stop at a signal, it adds 3 minutes to this journey time. Calculate his average speed, in kilometres per hour, if he stops at both road signals.

$$t = 18 + (2 \times 3) = 24 \text{ mins.}$$

$$= \frac{24}{60} \text{ hrs} = 0.4 \text{ hrs.}$$

$$s = \frac{12}{0.4} = 30 \text{ km/h}$$

.....30 kph [2]

- (d) Elsa takes a different route from Liverpool to Manchester. This route is 15 kilometres and there are no road signals. Elsa's average speed for this journey is 40 kilometres per hour. Find

i the time taken in minutes for this journey,

(e)

$$\frac{15}{40} \times 60 = 22.5 \text{ mins}$$

.....22.5 mins [1]

i the probability that Damon takes more time than this on his 12 kilometre journey.

Damon would take more time if he found 2 'stop' signals.

$$\therefore P = 0.6 \times 0.55 \\ = 0.33$$

.....0.33 [2]

4

$$x = \sqrt{b^3 c}$$

(a) Find the value of x when $b = 4$ and $c = 9$.

$$x = \sqrt{(4)^3 \times 9} = \sqrt{64 \times 9} \\ = 24$$

$x = 24$ [2]

(b) Rearrange the formula to write c in terms of x and b .

$$x^2 = b^3 c \\ \therefore c = \frac{x^2}{b^3}$$

$c = \frac{x^2}{b^3}$ [2]

5 Solve.

(a) $2(3 - 8x) = 54$

$$6 - 16x = 54$$

$$16x = -48$$

$$\therefore x = -3$$

..... $x = -3$ [2]

(b) $\frac{1}{y} = \frac{y+2}{3}$ (cross-multiply)

$$3 = y(y+2)$$

$$y^2 + 2y - 3 = 0$$

$$(y+3)(y-1) = 0$$

$$y = -3 \text{ or } y = 1$$

$y = -3$ or $y = 1$ [3]

6

$\Sigma f = 200$

200 students were asked how many hours they exercise each week.

The table shows the results.

Midpoint (x)	2.5	7.5	12.5	17.5	22.5	27.5	32.5	37.5
Time (t hours)	$0 < t \leq 5$	$5 < t \leq 10$	$10 < t \leq 15$	$15 < t \leq 20$	$20 < t \leq 25$	$25 < t \leq 30$	$30 < t \leq 35$	$35 < t \leq 40$
Number of students (f)	12	15	23	30	40	35	25	20

(a) Calculate an estimate of the mean.

$$\frac{\Sigma fx}{\Sigma f} = \frac{(12 \times 2.5) + (15 \times 7.5) + (23 \times 12.5) + (30 \times 17.5) + (40 \times 22.5) + (35 \times 27.5) + (25 \times 32.5) + (20 \times 37.5)}{200}$$

$$= \frac{4380}{200} = 21.9$$

..... 21.9 h[4]

(b) Use the information in the table above to complete the cumulative frequency table.

Time (t hours)	$t \leq 5$	$t \leq 10$	$t \leq 15$	$t \leq 20$	$t \leq 25$	$t \leq 30$	$t \leq 35$	$t \leq 40$
Cumulative frequency	12	27	50	80	120	155	180	200

+15 +23 +30 +40 +35 +25 +20

[1]

7 This question is about sequences.

(a) Find the 22nd term in the following sequence:

0th term
 -7
 $-2, 3, 8, 13, \dots$
 $+5 +5 +5 +5$
 $U_n = 5n - 7$
 $U_{22} = 5(22) - 7$
 $= 103$

.....103 [3]

(b) T_n is defined by the terms:

0.5, 1, 2, 4, ...

$\times 2 \times 2 \times 2$

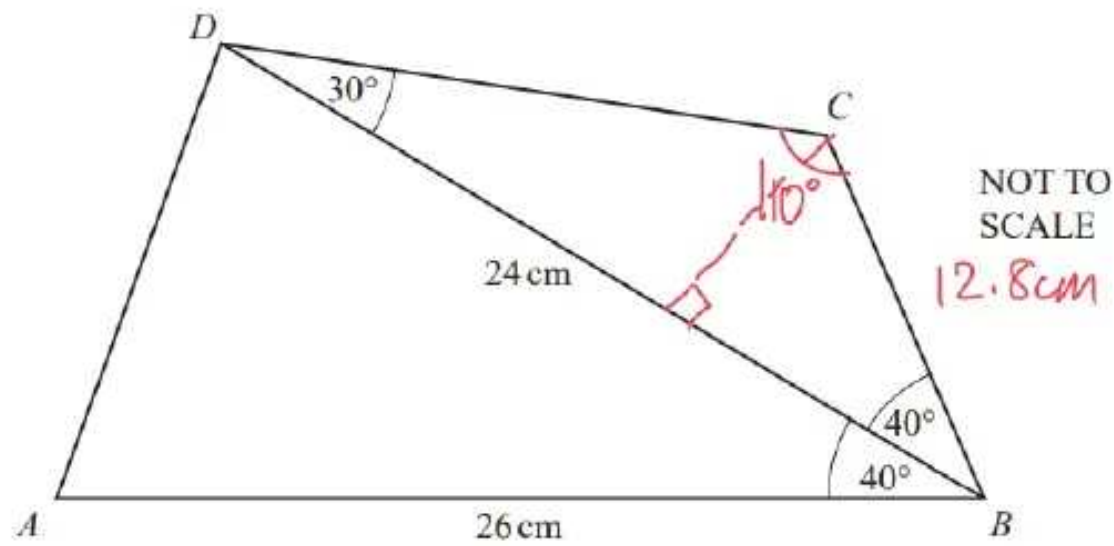
geometric progression

What is the smallest value of n for which T_n exceeds 875?

$ar^{n-1} \rightarrow 0.5 \times 2^{n-1}$
 $0.5 \times 2^{n-1} > 875$
 $2^{n-1} > 1750$
 $2^{10} = 1024, \quad 2^{11} = 2048$
 $\therefore n-1 = 11$
 $\Rightarrow n = 12$

$n =$12 [4]

8



$ABCD$ is a quadrilateral and BD is a diagonal.

$AB = 26$ cm, $BD = 24$ cm, angle $ABD = 40^\circ$, angle $CBD = 40^\circ$ and angle $CDB = 30^\circ$.

(a) Calculate the area of triangle ABD .

$$\frac{1}{2} \times 26 \times 24 \times \sin 40^\circ$$

$$= 201 \text{ cm}^2 \text{ (3 s. f.)}$$

.....201..... cm^2 [2]

(b) Calculate the length of AD .

$$AD^2 = 24^2 + 26^2 - 2(24)(26)\cos 40$$

$$AD = \sqrt{24^2 + 26^2 - 2(24)(26)\cos 40}$$

$$= 17.2 \text{ cm (3 s.f.)} \quad \dots\dots\dots 17.2 \text{ cm [4]}$$

(c) Calculate the length of BC .

$$\frac{BC}{\sin 30} = \frac{24}{\sin 110}$$

$$BC = \frac{24 \sin 30}{\sin 110} = 12.8 \text{ cm}$$

$$\dots\dots\dots 12.8 \text{ cm [4]}$$

(d) Calculate the shortest distance from the point C to the line BD . \rightarrow perpendicular

$$\sin 40 = \frac{x}{12.8}$$

$$x = 12.8 \times \sin 40 = 8.21$$

$$\dots\dots\dots 8.21 \text{ cm [2]}$$

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$$f(x) = x^2 - 4x + 3 \text{ and } g(x) = 2x - 3$$

(a) Solve $f(x) = 0$

$$x^2 - 4x + 3 = 0$$

$$(x-3)(x-1) = 0$$

$$x = 3 \text{ or } x = 1$$

$$\dots\dots\dots x = 3 \text{ or } x = 1 \dots\dots\dots [2]$$

(b) Find $g^{-1}(x)$

$$\text{Let } y = 2x - 3$$

$$x = \frac{y+3}{2}$$

$$x+3 = 2y \rightarrow y = \frac{x+3}{2} \rightarrow g^{-1}(x) = \frac{x+3}{2}$$

$$\dots\dots\dots \frac{x+3}{2} \dots\dots\dots [2]$$

(c) Solve $f(x) = g(x)$, giving each of your answers correct to 2 decimal places.

$$x^2 - 4x + 3 = 2x - 3$$

$$x^2 - 6x + 6 = 0$$

$$x = \frac{-(-6) \pm \sqrt{(-6)^2 - 4(1)(6)}}{2(1)}$$

$$x = 4.732 \dots$$

$$\text{or}$$

$$x = 1.267 \dots$$

$$x = 4.73 \dots \text{ or } x = 1.27 \dots [3]$$

- (d) Find $gf(-2x)$, simplifying your expression.

$$\begin{aligned}
 & \underbrace{g(f(-2x))}_{4g(f(-2x))} \\
 & (-2x)^2 - 4(-2x) + 3 \\
 & = 4x^2 + 8x + 3 \\
 \therefore g(4x^2 + 8x + 3) \\
 & = 2(4x^2 + 8x + 3) - 3 \\
 & = 8x^2 + 16x + 6 - 3 =
 \end{aligned}$$

$$\underline{8x^2 + 16x + 3} \dots\dots\dots [4]$$

- (e) Hence, or otherwise, find the value of $gf(4)$

$$\begin{aligned}
 -2x &= 4 \Rightarrow x = -2 \\
 8(-2)^2 + 16(-2) + 3 \\
 \therefore gf(4) &= 3
 \end{aligned}$$

$$\underline{3} \dots\dots\dots [2]$$

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- (a) Solve the equation $\sin x = 0.357$ for $0^\circ \leq x \leq 360^\circ$.

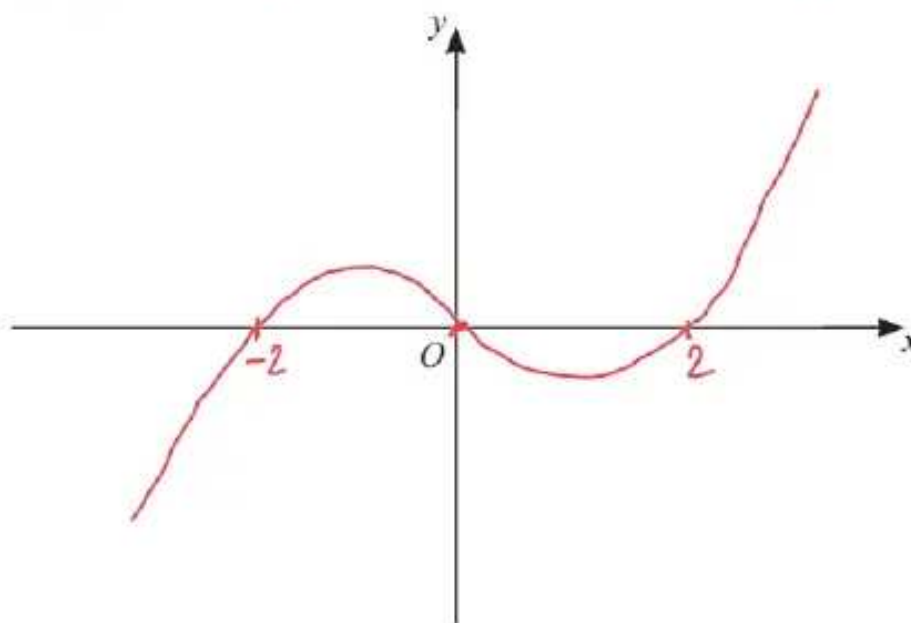
$$\begin{aligned}
 x &= \sin^{-1}(0.357) \\
 x &= 20.9 \\
 180 - 20.9 \\
 &= 159.1
 \end{aligned}$$



$$x = \underline{20.9} \dots\dots\dots \text{or } x = \underline{159.1} \dots\dots\dots [2]$$

- (b) Sketch the curve $y = x^3 - 4x$.

$$y = x(x^2 - 4) = x(x+2)(x-2)$$



coefficient of x^3 is +ve
 \hookrightarrow positive cubic



y intercept
 When $x=0$, $y=0$
 when $y=0$,
 $x=0$ or $x=2$ or
 $x=-2$
x intercepts

[3]

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- (c) A curve has equation $y = x^3 + px^2 + qx + r$

The stationary points of the curve occur when $x = 1$ and $x = -2$

Given that the curve passes through the point $(0, 4)$, work out the values of p , q and r .

$$\frac{dy}{dx} = 3x^2 + 2px + q$$

$$3(1)^2 + 2p(1) + q = 0 \Rightarrow 2p + q = -3 \quad \dots \textcircled{1}$$

$$3(-2)^2 + 2p(-2) + q = 0 \Rightarrow -4p + q = -12 \quad \dots \textcircled{2}$$

$$\textcircled{1} - \textcircled{2} \quad 6p = 9$$

$$\therefore p = \frac{3}{2}$$

Substituting $p = \frac{3}{2}$ into $\textcircled{1}$,

$$2\left(\frac{3}{2}\right) + q = -3$$

$$3 + q = -3$$

$$\hookrightarrow q = -6$$

$$y = x^3 + \frac{3}{2}x^2 - 6x + r$$

$$4 = (0)^3 + \frac{3}{2}(0)^2 - 6(0) + r$$

$$\therefore \underline{4 = r}$$

$$\therefore \underline{y = x^3 + \frac{3}{2}x^2 - 6x + 4}$$



$$\frac{3}{2}$$

$$-6$$

$$4$$

$p = \dots, q = \dots, r = \dots$ [8]

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